Voltage/Current Continuity
1)


In the above circuit, the voltage is defined as follows:
$V 1=\left\{\begin{array}{cc}5 V & t<0 \\ 10 V & 0<t\end{array}\right.$ (the voltage source changes from 5 V to 10 V at $\mathrm{t}=0$ )
a. Write V 1 in the format $\quad \ldots+($ or -$) \quad \__{\mathrm{u}}(\mathrm{t}) \quad$ (for example 2-2u(t))
b. At $\mathrm{t}=0$ - (just before the voltage changes), determine the voltage across each component and the current through each component (use the polarities indicated in the circuit). Draw the circuit.

| Component | Voltage | Current |
| :---: | :---: | :---: |
| R4 |  |  |
| R5 |  |  |
| R6 |  |  |
| C1 |  |  |

c.At $t=0+$ (just after the voltage changes), determine the voltage across each component and the current through each component for the polarities indicated in the circuit. Draw the circuit.

| Component | Voltage | Current |
| :---: | :---: | :---: |
| R4 |  |  |
| R5 |  |  |
| R6 |  |  |
| C1 |  |  |

2) First order circuits (Differential Equations)


In the above circuit, the source turns on at $t=0$ with a voltage of $15 \mathrm{~V}, \mathrm{Vs}=15 \mathrm{u}(\mathrm{t}) \mathrm{V}$. Additionally, at $\mathrm{t}=20 \mathrm{~s}$ the switch in series with C 2 is closed. You can (should) ignore C 2 for part a) of this problem.
a) For $0<t<20 \mathrm{~s}$, determine the voltage across C 1 as a function of time, $\mathrm{Vc}(\mathrm{t})$. If you do any circuit reduction/transformation, include a drawing of your circuit.
b) For $\mathrm{t}>20 \mathrm{~s}$, determine the votlage across C 1 as a function of time. Use the resistor and capacitor values in your solution. If you do any circuit reduction/transformation, include a drawing of your circuit.


In the above circuit, the source current is 20 mA for $\mathrm{t}<0$ and 0 for $\mathrm{t}>0$ (the source turns off at $\mathrm{t}=0$ ).
a) What is the initial $(\mathrm{t}=0+$ ) current through the inductor? What is the $(\mathrm{t}=0+)$ voltage across the inductor?
b) What is the DC steady state current through the inductor as $t->\infty$ ?
c) Symbolically, what is the differential equation defining the current through the inductor?
d) For $\mathrm{R} 1=100 \Omega$, determine the current through the inductor as a function of time for $\mathrm{t}>0$.
4) Second order, s-domain and Laplace


At $t=0, \mathrm{U} 1$ closes and U2 opens
a) Draw the s-domain equivalent circuit. Include all intial conditions and label your component values using symbolic notation (i.e. sL1)
b) Using impedances, determine the transfer function for the current through the capactor, C1. Use symbolic vlaues in your expression (R, L, C, I1, I2)
c) Find the current through the capacitor as a function of time for $\mathrm{R} 1=12.5 \mathrm{k}$. Is this circuit underdamped, overdamped or cricially damped.
d) Find the current through the capacitor as a functino of time for $\mathrm{R} 1=0.25 \mathrm{k}$. Is this circuit underdamped, overdamped or cricially damped.

